UNIVERSITY OF SASKATCHEWAN **ELECTRICAL ENGINEERING 455.3**

Assignment Quiz 7 November 21, 2001

Instructor: B.L. Daku Time: 15 minutes Aids: None

Name:

Student Number:

1. When the input to an LTI system is

$$x[n] = \left(\frac{1}{3}\right)^n u[n] + 2^n u[-n-1],$$

the corresponding output is

$$y[n] = 5\left(\frac{1}{3}\right)^n u[n] - 5\left(\frac{2}{3}\right)^n u[n].$$

- (a) Find the system function H(z) of the system. Plot the pole(s) and zero(s) of H(z)and indicate the region of convergence.
- (b) Find the impulse response h[n] of the system.
- (c) Write a difference equation that is satisfied by the given input and output.

(d) Is the system stable? Is it causal?

$$\chi(2) = \frac{1}{1 - \frac{1}{3} 2^{-1}} + \frac{-1}{1 - \frac{1}{2} 2^{-1}}$$

$$= \frac{\chi(2)^{-1} + \frac{1}{3} 2^{-1}}{(1 - \frac{1}{3} 2^{-1})(1 - \frac{1}{3} 2^{-1})}$$

$$= -\frac{\frac{5}{2} 2^{-1}}{(1 + \frac{1}{2} 2^{-1})(1 - \frac{1}{2} 2^{-1})}$$

$$y(2) = \frac{5}{1 - \frac{1}{3} \cdot 2^{-1}} + \frac{-5}{1 - \frac{2}{3} \cdot 2^{-1}}$$

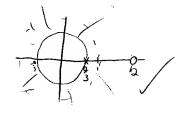
$$\frac{8 - \frac{9}{3} \cdot 2^{-1} - 8 + \frac{5}{2} \cdot 2^{-1}}{(1 - \frac{1}{3} \cdot 2^{-1})(1 - \frac{2}{3} \cdot 2^{-1})}$$

$$= \frac{-\frac{9}{3} \cdot 2^{-1}}{(1 - \frac{1}{3} \cdot 2^{-1})(1 - \frac{2}{3} \cdot 2^{-1})}$$

$$H(z) = \frac{-\frac{1}{3}z^{-1}}{\frac{(1-3z^{-1})(1-\frac{3}{2}z^{-1})}{(1-2z^{-1})(1-2z^{-1})}} \cdot \frac{(\frac{1}{3}z^{-1})(1-2z^{-1})}{\frac{2}{3}z^{-1}}$$

$$H(z) = \frac{-\frac{1}{3}z^{-1}}{(1-\frac{3}{3}z^{-1})} \cdot \frac{(\frac{1}{3}z^{-1})(1-2z^{-1})}{\frac{2}{3}z^{-1}}$$





ELECT

Exam File Provided By The VofS IEEE Student Branch

ieee.usask.ca

Name:

Aids: None

O

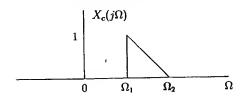
Student Number:

2)

Instructor: B.L. Daku

Time: 15 minutes

1. A complex-valued continuous-time signal, $x_c(t)$, has the Fourier transform shown in the following figure. The signal is sampled to produce the sequence $x[n] = x_c(nT)$.



- (a) Sketch the Fourier transform, $X(e^{j\omega})$, of the sequence x[n] for $T = \pi/\Omega_2$.
- (b) What is the lowest sampling frequency that can be used without incurring any aliasing distortion, i.e., so that $x_c(t)$ can be recovered from x[n]. Show your work. Sketch $X(e^{j\omega})$ using this sampling frequency.
- (c) Draw the block diagram of a system that can be used to recover $x_c(t)$ from x[n]if the sampling rate is greater than or equal to the rate determined in part b). Assume that (complex) ideal filters are available.

